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# **ARTICLE TYPE**

# Synthesis and characterisation of new $MO(OH)_2$ (M = Zr, Hf) oxyhydroxides and related $Li_2MO_3$ salts

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Two new solid  $MO(OH)_2$  (M = Zr, Hf) oxyhydroxides have been synthesised by an ion-exchange reaction from  $Li_2MO_3$  (M = Zr, Hf) precursors obtained by a citrate combustion technique. The crystal structure of the oxyhydroxides has been solved by a direct method and refined using Rietveld full profile

<sup>10</sup> fitting based on X-ray powder diffraction data. Both oxyhydroxides crystallize in a  $P2_1/c$  monoclinic unit cell and have a structure resembling that of the related salts. Detailed characterisation of the fine-structure features and chemical bonding in precursors and oxyhydroxide powders has been performed using vibrational spectroscopy, nuclear magnetic resonance spectroscopy, scanning electron microscopy, pair distribution function analysis and quantum-chemical modelling.

#### 15 Introduction

Solid oxyhydroxides have been intensively studied from the point of view of both fundamental science and potential applications. Natural oxyhydroxides (goethite, akaganeite, lepidocrocite, diaspore, boehmite and other minerals) [1-5] and synthetic <sup>20</sup> oxyhydroxides of 3d-transition metals (NiOOH, FeOOH, MnOOH, etc.) attract most of the attention because of their potential as materials for electrochemical energy storage [6-12], sensors [13], absorbents [14, 15] and electrochromic devices [16, 17].

- <sup>25</sup> However, in spite of active research in this field there are only a few reports concerning the synthesis and the characterisation of solid oxyhydroxides of the IVB group of the periodic table. Orera *et al.* reported on the synthesis of  $ZrO(OH)_2 \times 0.14H_2O$ oxyhydroxide from Li<sub>2</sub>ZrO<sub>3</sub> salt in aqueous solution of nitric
- <sup>30</sup> acid [18]. Denisova *et al.* described a method of synthesis and some properties of metatitanic acid  $H_2 TiO_3$  [19]. Yawata reported on the recovering of lithium ions from hot spring water using  $H_2 TiO_3$ , obtained from  $Li_2 TiO_3$  by ion exchange reaction [20]. Recently, we showed that all three MO(OH)<sub>2</sub> (M = Ti, Zr,
- <sup>35</sup> Hf) oxyhydroxides can be synthesised in solid form by ion exchange reaction in aqueous acetic acid solution from  $Li_2MO_3$ (M = Ti, Zr, Hf) precursors [19, 21-23]. It is worth to mention that the precursors in Refs. [19-23] have been obtained by standard solid state synthesis at temperatures 600-700°C [19, 21],
- <sup>40</sup> which are significantly lower than the temperatures used during the solid-state synthesis of the above-mentioned lithium salts [24-30]. In case of TiO(OH)<sub>2</sub> we showed that decreasing the synthesis temperature is crucial for obtaining oxyhydroxides. Indeed, only precursors annealed at low temperatures allow the
- <sup>45</sup> complete exchange of Li<sup>+</sup> by H<sup>+</sup> (the extent of exchange of lithium by protons in Li<sub>2</sub>TiO<sub>3</sub> obtained at 800-1000°C was found

to be less than 50%) [21, 22]. We proposed that this difference is probably caused by a high concentration of planar defects in the low-temperature modification of the  $Li_2TiO_3$  precursor [23].

<sup>50</sup> However, till now there are neither data concerning details of the crystal structure of precursors which present the possibility of an ion exchange reaction nor data concerning the crystal structure of  $MO(OH)_2$  (M = Zr, Hf). So far, only a crystallographic study of TiO(OH)<sub>2</sub> has been performed. Tarakina *et al.* [23] showed that <sup>55</sup> titanium oxyhydroxide belongs to the family of layered double hydroxides and can be described as a stacking of charge-neutral metal oxyhidroxide slabs [(OH)<sub>2</sub>OTi<sub>2</sub>O(OH)<sub>2</sub>]. It possesses a lot of disorder in the structure, partly preserved from the structure of the Li<sub>2</sub>TiO<sub>3</sub> precursor [23, 31, 32].

The main goal of this study is to solve the crystal structure of the new MO(OH)<sub>2</sub> (M = Zr, Hf) compounds using crystallographic information about the related lithium salt, obtained by a citrate synthesis. Our preliminary study and results published by Chai *et al.* [33] show that oxyhydroxides of the IVB <sup>65</sup> group of the periodic table have a high sorption affinity for polyvalent ions, including radioactive ions (Ag, Tl, As, Te, Sr, Th, U etc.). Therefore, knowledge of the crystal structure, bond formation, and acid-based properties of oxyhydroxides is essential for understanding the physico-chemical properties of <sup>70</sup> these compounds and will be of help in guiding the design of potential applications.

In addition, the citrate synthesis routine proposed in this work for the synthesis of precursors should lead to a considerable reduction of the synthesis temperature and, probably, the size of 75 the particles in the obtained  $\text{Li}_2\text{MO}_3$  (M = Zr, Hf) powders which can be interesting not only with respect to the synthesis of  $\text{MO}(\text{OH})_2$  (M = Zr, Hf). For example,  $\text{Li}_2\text{ZrO}_3$  was recently proposed as a potential CO<sub>2</sub> absorber material, because of its high capture capacity for carbon dioxide, high stability, and ease of regeneration [34-40]. The need for obtaining this salt with a large surface area (smaller size of the grains) and at lower costs (at lower temperatures) draws the attention to combustion methods for the synthesis of  $Li_2ZrO_3$  [37-41].  $Li_2HfO_3$  is less studied and has been considered as a full structural analogue of

<sup>5</sup> studied and has been considered as a full structural analogue of  $Li_2ZrO_3$  [28-30]. However, in recent work of Baklanova *et al.* the presence of an extra line in the cathodoluminescence spectrum of  $Li_2HfO_3$  obtained by the citrate method has been revealed; this raises the question of full structural analogy <sup>10</sup> between the above-mentioned salts again [42].

# Experiment

#### Synthesis

 $MO(OH)_2$  (M = Zr, Hf) powders were synthesised from  $Li_2MO_3$  (M = Zr, Hf) precursors by ion exchange reactions.

- <sup>15</sup> Synthesis of Li<sub>2</sub>ZrO<sub>3</sub> and Li<sub>2</sub>HfO<sub>3</sub> precursors. For the synthesis of the Li<sub>2</sub>ZrO<sub>3</sub> precursor a stoichiometric amount of  $Zr(OH)_2CO_3 \times 5.5$ -6.0H<sub>2</sub>O (99,9%) and Li<sub>2</sub>CO<sub>3</sub> (99,9%) was dissolved in a nitric acid solution HNO<sub>3</sub> (2M). The obtained solution was steamed at 250°C to remove remains of nitric acid.
- <sup>20</sup> Citric acid (C<sub>6</sub>H<sub>8</sub>O<sub>7</sub>·2H<sub>2</sub>O) powder was added to the solution, which then was boiled down till the formation of a dry residual solid. Calcination of the precipitate was performed in several steps in the temperature range 300-780°C with intermediate cooling and regrinding at each stage. Particular details of the <sup>25</sup> synthesis of Li<sub>2</sub>ZrO<sub>3</sub>by citrate combustion method can be found
- in Ref. [43].

 $Li_2CO_3$  (99.9%) and  $HfO_2 \times 4.5H_2O$  were used as starting compounds for the synthesis of the  $Li_2HfO_3$  precursor. Initially, fresh  $HfO_2 \times 4.5H_2O$  powder was synthesized. For this,  $HfO_2$ 

- <sup>30</sup> (99.9%) was dissolved in a water solution of hydrofluoric acid (40 mass%). The obtained solution was steamed for a long time in order to remove remaining fluoride ions and then 10 times diluted with distilled water. A  $NH_4OH$  solution (12.5 mass%) was added to the reaction mixture. The latter was kept during 4-5
- $_{35}$  hours at room temperature in order to reach complete precipitation of Hf ions in a hydrated form. The obtained gel was separated from the solution by decantation, washed several times in distilled water, filtered and dried in air. Then, the freshly synthesized HfO\_2×4.5H\_2O powder was dissolved in diluted
- <sup>40</sup> HNO<sub>3</sub> (2M) with continual stirring and heating at 150°C; a stoichiometric amount of  $Li_2CO_3$ , and an amount of  $C_6H_8O_7$ ·2H<sub>2</sub>O citric acid sufficient for complex formation, were added to the reaction mixture. The obtained solution was then heated at ~250°C under constant stirring till the formation of a
- <sup>45</sup> dry residual solid. Calcining of the residual solid powder was performed in three steps at the temperature 300°C (2 hours), 650°C (10 hours) and 700°C (4 hours), with intermediate cooling and regrinding in an agate mortar at each stage.

Synthesis of  $MO(OH)_2$  (M = Zr, Hf).  $MO(OH)_2$  (M = Zr, Hf) <sup>50</sup> oxyhydroxides were synthesised from  $Li_2MO_3$  (M = Zr, Hf) precursors by ion exchange reactions in an acetic acid aqueous solution (0.05 mol/l) at a temperature of 60°C during 14 hours. The extent of exchange of  $Li^+$  by H<sup>+</sup> was controlled using a pHmeter (Anion 4100) with glass electrode. The ratio between solid

ss and liquid phases was 1g/1l. The final product, MO(OH)<sub>2</sub> (M = Zr, Hf), was washed in distilled water and dried in air till constant

mass was achieved.

#### **Characterization techniques**

The elemental compositions of the samples were determined <sup>60</sup> by an emission spectral analysis (ESA) using an Optima 4300 DV with inductively coupled plasma (Zr and Hf contents) and by atomic absorption spectroscopy in an acetylene-air flame using a Perkin-Elmer 503 spectrometer (Li content).

X-ray powder diffraction (XRD) patterns were collected at room temperature on a transmission STADI-P (STOE, Germany) diffractometer equipped with a linear mini-PSD detector using Cu  $K_{\alpha l}$  radiation in the 20 range 2° - 120° with a step of 0.03°. Polycrystalline silicon (a = 5.43075(5) Å) was used as an external standard. The phase purities of the samples were checked by ro comparing their XRD patterns with those in the Powder diffraction file - PDF2 database (ICDD, USA, release 2010). The GSAS program package [44, 45] was used for structure refinement from powder data.

Synchrotron radiation scattering experiments were carried out <sup>75</sup> at BW5 (DESY, Hamburg, Germany) at a primary energy of 100 keV, i.e. a wavelength of 0.123984 Å, using a Perkin-Elmer flat panel area detector at room temperature. The samples were loaded into a capillary with outer diameter equal to 1.8 mm. For background corrections a spectrum from an empty capillary with <sup>80</sup> the same diameter was collected. Refinement of the pair distribution function (PDF) data was carried out with the PDFgui [46] and DISCUS [47] software packages.

The morphology of the obtained powders was studied using a FEI Helios Nanolab Dual Beam system and a JEOL JSMss 6390LA scanning electron microscope. Transmission electron microscopy (TEM) studies were carried out using a FEI Titan 80-300 (S) TEM operated at 300 kV. Particle size distributions of the obtained samples were evaluated from SEM images, collected in histogram form and fitted to log-normal distributions.

Nuclear magnetic resonance (NMR) <sup>1</sup>H high-resolution spectra were recorded using a Bruker AVANCE AV 300 spectrometer with sample rotation frequency 18 kHz.

Raman measurements were performed at room temperature on a RENISHAW U1000 spectrometer under  $Ag^+$  laser excitation ( $\lambda$  <sub>95</sub> = 514.5 nm).

For collecting infra red (IR) absorption spectra, powder samples were mixed with caesium iodide (CsI) and pressed into pellets. Spectra were recorded using an IR Fourier spectrometer Vertex 80 (Bruker) in the 400-4000 cm<sup>-1</sup> frequency range.

#### Quantum-chemical calculations

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Quantum-chemical calculations of monoclinic (sp.gr. C2/c) lithium metallates Li<sub>2</sub>MO<sub>3</sub> (M = Zr, Hf) were performed using a 24-atom unit cell. Relaxed atomic positions were obtained by <sup>105</sup> minimizing the total energy of the system while keeping the lattice parameters of Li<sub>2</sub>ZrO<sub>3</sub> and Li<sub>2</sub>HfO<sub>3</sub> fixed at their experimental values (Table 1). The calculations were performed in the framework of density functional theory (DFT) *ab initio* molecular dynamics (MD) with the SIESTA code [48], where <sup>110</sup> pseudo-atomic orbitals are constructed by means of firstprinciples norm-conserving pseudopotentials [49]. For the exchange-correlation potential the generalized-gradient approximation in the formulation of Perdew, Burke and Ernzerhof (GGA-PBE) was taken [50]. The calculations of the total energy and of the forces on each atom were performed with precisions of 0.1 meV and 0.5 meV/Å, respectively. For the construction of the pseudopotentials, the following cut-off atomic  $_{5}$  orbital radii were used: Li (2s) – 2.00 a.u., (2p) – 2.23 a.u.; O – (2s) – 2.00 a.u., (2p) – 1.30 a.u.; Zr – (5s) – 2.00 a.u., (5p) – 3.00 a.u., (4d) – 2.82 a.u. Hf – (6s) – 2.00 a.u., (6p) – 2.78 a.u., (5d) – 2.78 a.u. and for H – 1.25 a.u. All calculations were performed with a double zeta basis set with charge polarisation taken into 10 account and with an energy cut-off of 300 eV. The equilibrium

atomic positions were determined by minimizing the total energy

by means of the Parrinello-Rahman algorithm [51].

### **Results and Discussion**

#### Li<sub>2</sub>MO<sub>3</sub> (M = Zr, Hf) precursors

<sup>15</sup> In our previous works [21, 22] we have shown that the extent of exchange of  $\text{Li}^+$  by  $\text{H}^+$  for  $\text{Li}_2\text{MO}_3$  (M = Ti, Zr) compounds obtained bysolid state synthesis is significantly higher if the precursors were calcined at lower temperatures. In the present work,  $\text{Li}_2\text{ZrO}_3$  has been synthesised using a citrate synthesis <sup>20</sup> (Table 1).

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		Li <sub>2</sub> ZrO <sub>3</sub>	Li <sub>2</sub> HfO <sub>3</sub>	ZrO(OH) <sub>2</sub>	HfO(OH) <sub>2</sub>
Synthesis literature <sup>a</sup>		$T = 400^{\circ}C, 650^{\circ}C;$	-	-	-
conditions		$t_{total} \approx 18$ hours [40]			
	present work	T = 300°C, 650°C, 700°C;	T = 300°C, 650°C, 700°C	$T = 60^{\circ}C;$	$T = 60^{\circ}C;$
		$t_{total} \approx 16$ hours	$t_{total} = 16$ hours	$t_{total} \approx 14 \text{ hours}$	$t_{total} \approx 14 \text{ hours}$
Partic	ele size	360±150nm	86±37 nm	400±120nm	92±35nm
Crystal structure	Unit cell	a = 5.4283(1)Å	a = 5.4149(2)Å	a = 5.5996(8)Å,	a = 5.5578(5)Å,
data	parameters <sup>b</sup>	b = 9.0297(6)Å	b = 8.9795(3)Å	b = 9.2928(14)Å,	b = 9.0701(10)Å,
		c = 5.4232(1)Å	c = 5.3991(2)Å	c = 5.6993(8)Å,	c = 5.7174(5)Å,
		$\beta = 112.72(1)^{\circ}$	$\beta = 112.83(1)^{\circ}$	$\beta = 119.152(9)^{\circ}$	$\beta = 119.746(5)^{\circ}$
	$R_{\rm wp}, R_{\rm p}, R(F^2), \%$	8.14, 6.26, 7.93	8.66, 6.17, 8.25	3.81, 2.86, 0.99	3.64 2.65, 2.45

Table 1 Synthesis conditions and crystal structure data of  $Li_2MO_3$  (M = Zr, Hf) precursors and MO(OH)<sub>2</sub> (M = Zr, Hf) oxyhydroxides.

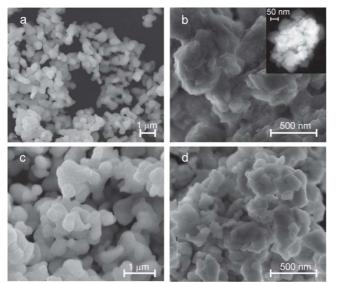
<sup>*a*</sup> Literature data in case of Li<sub>2</sub>MO<sub>3</sub> (M=Zr, Hf) are given only for combustion method of synthesis. <sup>*b*</sup>Li<sub>2</sub>MO<sub>3</sub> (M=Zr, Hf) crystallized in sp.gr. C2/c, MO(OH)<sub>2</sub> in sp.gr. P2<sub>1</sub>/c.

Table 2 Atomic coordinates and isotropic thermal parameters for  $Li_2MO_3$  (M = Zr, Hf) obtained by citrate combustionsynthesis.

Atom	x/a	y/b	z/c	Occupancy	U <sub>iso</sub> >	<100, Å <sup>2</sup>
M/Li	0	0.09029(16) 0.08992(26)	0.25	0.932(8)/0.068(8) 0.804(9)/0.191	9) 1.56	3.18(13)
Li1/M1	0	0.4208(18) 0.4167(15)	0.25	0.974(1)/0.026(1) 0.886(3)/0.114(	3) 1.76	3.06(30)
Li2/M2	0	0.7403(26) 0.7528(27)	0.25	1.0 0.963(2)/0.037(	1) 2.14	2.00(60)
O1	0.25	0.25	0.5	1.0	1.66	2.5
02	0.2732(6) 0.2790(13)	0.5743(5) 0.5711(10)	0.4841(7) 0.4913(14)	1.0	2.23	2.5

25 Data for Li<sub>2</sub>HfO<sub>3</sub> are given in *italic*.

30



**Fig. 1** SEM and TEM images of Li<sub>2</sub>ZrO<sub>3</sub> (a) and Li<sub>2</sub>HfO<sub>3</sub> (b) precursors obtained by the citrate synthesis and ZrO(OH)<sub>2</sub> (c) and HfO(OH)<sub>2</sub> (d) oxyhydroxides synthesized from them.

In both solid-state and citrate synthesis methods a temperature

of T = 700 °C was found to be thermodynamically essential for the formation of homogeneous polycrystalline Li<sub>2</sub>ZrO<sub>3</sub>. However, the application of the citrate synthesis method <sup>35</sup> significantly influences on the kinetics of the phase formation, allowing to obtain a Li<sub>2</sub>ZrO<sub>3</sub> polycrystalline powder four times faster (Table 1).A noticeable change was also observed in the time required for the ion exchange reaction to complete. Thus, the formation of ZrO(OH)<sub>2</sub> takes place three times slower (44 hours) <sup>40</sup> when the precursor prepared by the solid state method is used. For ZrO(OH)<sub>2</sub> precursors obtained by citrate method complete

For  $ZrO(OH)_2$  precursors obtained by citrate method complete exchange observed already after 14 hours (Table 1). Taking this into consideration, only precursors obtained by the citrate method have been used for the synthesis of HfO(OH)<sub>2</sub>.

<sup>45</sup> The morphology of the obtained compounds was studied using SEM and TEM. Li<sub>2</sub>ZrO<sub>3</sub> and Li<sub>2</sub>HfO<sub>3</sub> obtained by the citrate method contain agglomerates (up to 0.5 μm) typical for combustion synthesis techniques; these agglomerates consist of small lamellar particles with an average particle size of 360±150
<sup>50</sup> nm and 86±37 nm, respectively (Table 1). The value for Li<sub>2</sub>ZrO<sub>3</sub> corresponds well with results reported by Xiao *et al.* [40]. During the ion exchange reaction, particle size is typically preserved, so that the oxyhydroxides consist of particles of almost the same size and shape as the starting precursors (Table 1, Fig 1). SEM
<sup>55</sup> and TEM images of precursors and oxyhydroxides are shown in

Fig. 1.

The XRD patterns of Li<sub>2</sub>ZrO<sub>3</sub> and Li<sub>2</sub>HfO<sub>3</sub> obtained by the citrate synthesis are shown in Figure 2. An analysis of

systematically absent reflections (hk0: h+k = 2n; h0l: h = 2n, l = 5 2n; 0k0: k = 2n) in the XRD patterns indicates two possible space groups, *Cc* and *C*2/*c*, for both compounds.

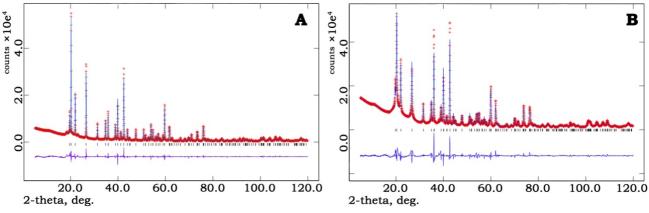
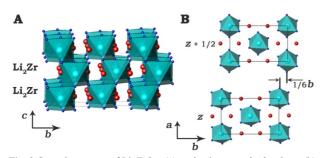


Fig. 2 XRD patterns of (a) Li<sub>2</sub>ZrO<sub>3</sub> and (b) Li<sub>2</sub>HfO<sub>3</sub> precursors obtained by the citrate combustion synthesis.

- <sup>10</sup> The structure of Li<sub>2</sub>ZrO<sub>3</sub> [24] was used as a starting model for the refinement. The peak profiles were fitted with a pseudo-Voigt function,  $I(2\theta) = x^*L(2\theta) + (1-x)^*G(2\theta)$  (where *L* and *G* are the Lorentzian and Gaussian part, respectively). The angular dependence of the peak width was described by the relation <sup>15</sup> (FWHM)<sup>2</sup> =  $Utg2\theta + Vtg\theta + W$ , where FWHM is the full line width at half maximum. The background level was described by a 36-order Chebyshev polynomial. The absorption correction function for a flat plate sample in transmission geometry has been applied. At the final steps of refinement mixed occupancies of the
- <sup>20</sup> metal sites were introduced. This does not influence on the quality of the refinement in case of Li<sub>2</sub>ZrO<sub>3</sub>, but considerably reduces the reliability factors for the refinement of Li<sub>2</sub>HfO<sub>3</sub>. The crystallographic data, *R*-values and selected interatomic distances are given in Tables 1, 2, 3.
- Li<sub>2</sub>ZrO<sub>3</sub> and Li<sub>2</sub>HfO<sub>3</sub>salts are isostructural and can be described as a cubic close-packing of oxygen atoms in the octahedral voids between which metals are placed. Only one type of mixed metal layer with a honeycomb arrangement of Li atoms is formed. In the unit cell, two layers are stacked on top of each <sup>30</sup> other along the *c* axis with a 1/6 shift along the *b* direction (Fig. 3).

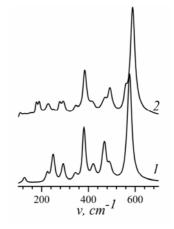


**Fig. 3** Crystal structure of Li<sub>2</sub>ZrO<sub>3</sub>: (a) projection onto the *bc* plane, (b) projection onto the *ab* plane. Li, Zr and O are drawn as red, light-blue and blue spheres respectively.

For both oxides the profile fit of XRD patterns is not perfect: the intensities of some reflections (021, -202, -131, 131, *etc.*) are

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not described correctly and a non-uniform broadening of the <sup>40</sup> peaks in the 2θ range 18-40° is observed. In spite of a considerable decrease of the *R*-values for Li<sub>2</sub>HfO<sub>3</sub> after introduction of mixed occupancies of the metal positions, the above-mentioned issues of profile refinement remain unsolved. Moreover, the chemical composition obtained from the <sup>45</sup> refinement is Li<sub>2.04</sub>Hf<sub>0.96</sub>O<sub>3</sub>, which is different from the nominal one. These facts indicate serious limitations of the presented fit. A more complex approach has to be proposed in order to control the refinement process better, probably the lamellar shape and the small size of the particles have to be included, as well as possible <sup>50</sup> structural defects, as demonstrated for the Li<sub>2</sub>TiO<sub>3</sub> compound [23, 31, 32].



**Fig.4** Raman spectra of (1)  $\text{Li}_2\text{ZrO}_3$ ,(2)  $\text{Li}_2\text{HfO}_3$ .

Similarity in positions and intensity of the lines on the Raman ss spectra of the  $Li_2MO_3$  (M = Zr, Hf) salts indicates that these compounds are isostructural. Lines in the spectral range 500 - 600 cm<sup>-1</sup> correspond to symmetrical stretching vibrations of Zr–O and Hf–O bonds [29, 30]. The ~ 14 cm<sup>-1</sup> shift of Hf–O lines to the high frequency spectral range in  $Li_2HfO_3$  compared with the 60 positions of analogous lines in isostructural  $Li_2ZrO_3$  can be explained by shorter bond lengths in the former (Table 3). Lines at 350 - 400 cm<sup>-1</sup>are associated symmetrical stretching vibrations of Li–O bonds, while lines at 400 - 500 cm<sup>-1</sup> and 150 - 350 cm<sup>-1</sup> – can be attributed to both stretching and bending vibrations of all M-O bonds.

- <sup>5</sup> In order to reveal the chemical bonding characteristics and their dependence on the electronic structure of the  $M^{4+}$  ion which forms the salt and on the position of the Li<sup>+</sup> atoms to be substituted by H<sup>+</sup> atoms, *ab initio* calculations have been performed for salts with the following compositions: Li<sub>2</sub>MO<sub>3</sub>
- <sup>10</sup> and  $Li_{1.5}H_{0.5}MO_3$  (M= Zr, Hf). The obtained interatomic distances in MO<sub>6</sub> and LiO<sub>6</sub> octahedra for  $Li_2MO_3$  and  $Li_{1.5}H_{0.5}MO_3$  are given in Table 3. In both hafnium salts, the calculated M O distances are shorter and Li O distances are longer than the corresponding distances in zirconium salts.

15 **Table 3** Selected interatomic distances (Å) for  $Li_2MO_3$  (A = Zr, Hf).

	1:7	·	T : T	IfO
	Li <sub>2</sub> Z	2	Li <sub>2</sub> H	2
Bond	XRD	Ab initio	XRD	Ab initio
M–O(1) ×2	2.0828(10)	2.0869	2.0739(16)	2.0611
M-O(2) ×2	2.0872(34)	2.1131	2.090(7)	2.0833
M-O(2) ×2	2.106(4)	2.1323	2.039(8)	2.1038
	2.092	2.111	2.067	2.083
	0.008	0.015	0.018	0.015
	0.154(10)	2 1000	0.114(0)	2 1 5 9 5
Li1–O(1) ×2	2.154(12)	2.1808	2.114(9)	2.1585
Li1-O(2) ×2	2.068(12)	2.0580	2.089(12)	2.0364
Li1-O(2) ×2	2.4356(33)	2.3463	2.427(7)	2.3687
	2.219	2.195	2.21	2.188
	0.123	0.093	0.121	0.109
Li2-O(1) ×2	2.2603(9)	2.2291	2.2523(2)	2.2252
Li2-O(2) $\times 2$	2.146(17)	2.2210	2.261(18)	2.2034
Li2-O(2) $\times 2$	2.241(18)	2.1316	2.152(19)	2.1176
, í	2.215	2.193	2.222	2.182
	0.039	0.035	0.039	0.046

*Note.* Average values are given in boldface, the relative degree of distortion<sup>‡</sup> of octahedral in italic.

From XRD and *ab initio* calculations one can conclude that Li1 octahedra are the most distorted ones in both compounds and <sup>20</sup> that, on average, Li<sub>2</sub>HfO<sub>3</sub> displays more distortion in polyhedra than Li<sub>2</sub>ZrO<sub>3</sub>. Substitution of 25% lithium atoms by hydrogen leads to further distortion of MO<sub>6</sub> octahedra.

<b>Table 4</b> Bond lengths in M <sup>4+</sup> O <sub>6</sub> octahedra depending on the atomic
position of Li substituted by hydrogen in $Li_{1.5}H_{0.5}MO_3$ (M = Zr, Hf).

1	-			, ,
	Н —	Li1	${ m H}$ $ ightarrow$	Li2
	M1	M2	M1	M2
$Zr-O(1) \times 2$	2.0346	2.0442	2.1018	2.0472
$Zr-O(2) \times 2$	2.1208	2.0786	2.0706	2.0632
$Zr-O(2) \times 2$	2.1623	2.2325	2.1242	2.2576
	2.1059	2.1184	2.0989	2.1227
	0.0619	0.0947	0.0257	0.1104
$Hf-O(1) \times 2$	2.0062	2.0114	2.0911	2.0302
Hf-O(2) ×2	2.0914	2.0529	2.0376	2.0446
$Hf-O(2) \times 2$	2.1371	2.2075	2.1066	2.2207
	2.0782	2.0906	2.0784	2.0985
	0.0639	0.0989	0.0348	0.1011

25 *Note.* Average values are given in boldface, the relative degree of distortion<sup>+</sup> of octahedral is given in italic.

It has been found that  $H^+$  ions which substitute  $Li^+$  to form  $Li_{1.5}H_{0.5}MO_3$  salts are considerably shifted from the corresponding Li1 or Li2 positions, which means that one H-O <sup>30</sup> bond in the hypothetic {HO<sub>6</sub>} octahedra is significantly shorter than the others and probably particularly this bond forms the OH-

group. Such shift broadens the natural structural channels formed by  $MO_6$  octahedra, which can create a favourable condition for subsequent exchange of  $Li^+$  by  $H^+$ .

**Table 5** The shortest O-H bond lengths in  $Li_{1,5}H_{0,5}MO_3$  (M = Zr, Hf)

	O - H bond, (Å)			
$H^+ \rightarrow Li^+$	Li <sub>2</sub> ZrO <sub>3</sub>	Li <sub>2</sub> HfO <sub>3</sub>		
Li1	1.2482	1.2507		
Li2	1.2514	1.2453		

#### $MO(OH)_2$ (M = Zr, Hf) oxyhydroxides

35

The diffraction patterns of ZrO(OH)2 and HfO(OH)2 have 40 been indexed in a  $P2_1/c$  monoclinic space group with unit cell constants a = 5.5996(8) Å, b = 9.2928(14) Å, c = 5.6993(8) Å,  $\beta$ =  $119.152(9)^{\circ}$  and a = 5.5578(5) Å, b = 9.0701(10) Å, c =5.7174(5) Å,  $\beta = 119.746(5)^\circ$ , respectively. The oxyhydroxides 45 are isostructural. The crystal structure of HfO(OH)2 has been solved using the EXPO2009 program suite [52]. This solution shows that HfO(OH)<sub>2</sub> keeps the basic motive of the related Li<sub>2</sub>HfO<sub>3</sub> salt [28]. The pairs of Hf octahedra remain preserved in the structure of the oxyhydroxide. However, their rotation in the 50 ab plane destroys the oxygen close-packed arrangement and leads to a lowering of the symmetry of the structure. The obtained model was used as a starting model for the refinement of the crystal structure of both ZrO(OH)<sub>2</sub> and HfO(OH)<sub>2</sub>. It is worth to mention that the XRD patterns of both oxyhydroxides show 55 significant broadening of Bragg reflections. This broadening can be due to several reasons: lamellar shape of the particles, size of the particles, stacking faults, poor crystallinity, etc. In order to describe this broadening, a profile function that employs a multiterm Simpson's rule integration of the pseudo-Voigt function has 60 been used [44, 53, 54]. Application of this function enables describing the profile when one set of reflections has a different particle size anisotropy than another set. This effect can be found on the diffraction patterns of e.g. samples with stacking faults, broadening some reflections and leaving a sublattice of sharp 65 reflections unmodified through the stacking fault. The calculated, observed and difference XRD patterns are shown in Fig. 5. The refined atomic coordinates, temperature factors and selected interatomic distances are given in Tables 6 and 7.

Vibrational spectra of MO(OH)<sub>2</sub> (M = Zr, Hf) are given in <sup>70</sup> Figure 4. Lines at 530-590 cm<sup>-1</sup>, which correspond to stretching vibrations of Zr–O and Hf–O bonds, split into two components of different intensity. This fact indicates a significant distortion of the MO<sub>6</sub> (M = Zr, Hf) octahedra and an extension of the M–O bonds during the substitution of Li<sup>+</sup> ions by protons in the crystal <sup>75</sup> structure of salts. The Raman spectrum of HfO(OH)<sub>2</sub> consist of more splitted lines than ZrO(OH)<sub>2</sub>, which indicates that the structure of the former is less symmetric. This fact agrees well with crystallographic data obtained from XRD of oxyhydroxides and *ab initio* calculations for partly substituted Li<sub>1.5</sub>H<sub>0.5</sub>MO<sub>3</sub> <sup>80</sup> phases. Significant broadening of the peaks in the spectrum of HfO(OH)<sub>2</sub>, in addition to the SEM, TEM and XRD measurements confirms the small particle size of the hafnium oxyhydroxide. The stretching vibrations of the O-H bond results in lines in the high-frequency range of the spectra of MO(OH)<sub>2</sub> (M = Zr, Hf). The occurrence of broad asymmetric lines at 3400 and 3500 cm<sup>-1</sup> in the spectrum of  $ZrO(OH)_2$  and  $HfO(OH)_2$ ,

respectively, indicates the presence of two non-equivalent 5 positions of the OH-groups in the crystal structure

Atom	x/	a	у	/b	Z	z/c	$U_{iso} \times 100 (\text{\AA}^2)$
М	0.7187(9)	0.7235(5)	0.1064(3)	0.10294(19)	-0.0315(6)	-0.04625(35)	2.50
O1	0.8361(44)	0.805(4)	-0.0176(23)	-0.0658(31)	-0.2107(35)	-0.1954(31)	2.50
O2 (OH)	0.3144(40)	0.314(4)	0.0667(21)	0.0396(22)	-0.1592(30)	-0.2279(30)	2.50
O3 (OH)	0.4890(24)	0.668(4)	0.1524(20)	0.1535(19)	-0.4821(26)	-0.4753(40)	2.50
O4	-0.0286(33)	-	0.2755(18)	-	0.2510(24)	-	2.50

Table 6 Atomic coordinates and isotropic thermal parameters for MO(OH)<sub>2</sub> (M = Zr, Hf).

Note. Data for HfO(OH)<sub>2</sub> are given in *italic*; occupancies are equal to 1 for all atoms, except for O4 for which it is equal to 0.957(25).

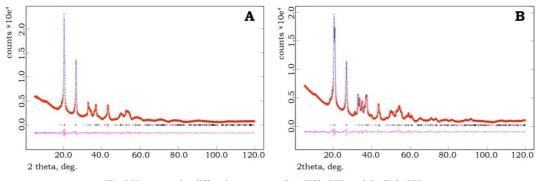


Fig.5 X-ray powder diffraction patterns of (a) HfO(OH)<sub>2</sub> and (b) ZrO(OH)<sub>2</sub>.

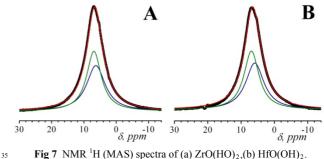
A B 2 2 1 600 3600 200 400 3200 2800 v, cm<sup>-1</sup> v, cm<sup>-1</sup>

10

Fig. 6 Raman (A) and IR (B) spectra of (1) ZrO(OH)<sub>2</sub>,(2) HfO(OH)<sub>2</sub>. 15

This fact is additionally confirmed by <sup>1</sup>H NMR measurements, where the <sup>1</sup>H NMR signal of the oxyhydroxides appears as the superposition of two lines with different values of chemical shifts: 6.9, 6.3 ppm and 6.9, 5.9 ppm for ZrO(OH)<sub>2</sub> and 20 HfO(OH)2, respectively, indicating two different crystallographic positions of the OH-groups (Fig 6). Both the smaller value of the chemical shift for HfO(OH)<sub>2</sub> and the appearance of lines for stretching vibrations in the high frequency range of IR spectrum point to a stronger base nature of the hydroxyl groups in 25 HfO(OH)<sub>2</sub> compared to ZrO(OH)<sub>2</sub>. Probably, this fact, together with shorter Hf-O bond lengths, allows to conclude that

HfO(OH)<sub>2</sub> is the thermally most stable among the oxyhydroxides formed by elements of the IVB group (Ti, Zr, Hf) of the periodic table [21, 23]. From another point of view, the stronger base 30 nature of the OH-groups in combination with the nanosize of the particles can also be responsible for the much more rapid HfO(OH)<sub>2</sub> formation during the ion exchange reaction compared to ZrO(OH)<sub>2</sub>.





Unfortunately, the  $MO(OH)_2$  (M = Zr, Hf) oxyhydroxides are not stable under a high voltage electron beam, therefore their local structure cannot be studied directly using transmission electron microscopy techniques. Since HfO(OH)<sub>2</sub> was found to be 40 more dispersed than ZrO(OH)2, we tried the same structural models to fit the experimental PDF for HfO(OH)<sub>2</sub> in order to get more details on its particle size and its local structure. The PDF technique, similar to the Rietveld refinement, uses a least-squares procedure to compare experimental and model data (PDF) 45 calculated from a proposed structural model. Unit cell constants, atomic coordinates, thermal factors, instrument parameters and the average size of coherently scattering domains (as a spherical particle) have been included in the refinement. The model PDF was convoluted with a Sinc function [55] before comparing with

experimental results in order to take into account the finite  $Q_{\text{max}}$  s of the diffraction data.

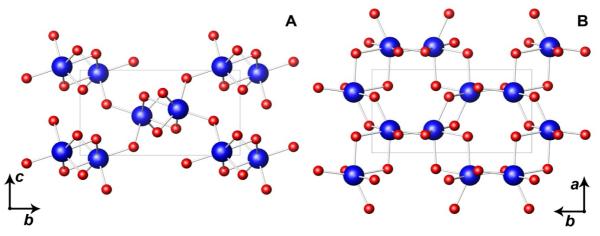


Fig. 8 Crystal structure of  $MO(OH)_2$  (M=Zr, Hf), projected on the *bc* (a) and the *ab* (b) plane. Zr(Hf) and O are drawn as blue and red spheres, respectively.

The model obtained from X-ray powder diffraction data gives a <sup>10</sup> good description of the PDF data in the range r = 1-30 Å, (especially at the *r* values up to 8Å, Figure 9b). In order to describe the experimental PDF at higher values of *r*, a domain size has been introduced into the refinement, resulting in convergence at about 70 Å, but considerably worsening the fit at

- <sup>15</sup> small *r*. This fact indicates the presence of disorder, which can be related to the lamellar shape of the particles. It is worth to mention that the distortion of Hf octahedra was found to be 0.09 from refinement of the whole set of PDF data and 0.19 from the first 8Å of the pattern, while the value obtained from Rietveld
- 20 refinement is 0.18 (Table 7). This difference in octahedral distortion indicates that the distortion differs between different domains.

This can be the evidence of size and shape dependence which is described by the PDF analysis more correctly. Summarising we

25 can say that the presence of disorder in the precursor is most probably retained in the structure of the oxyhydroxide. An additional neutron experiment is essential to get a correct description of disorder and to determine the positions of the hydrogen atoms.

<sup>30</sup> 

	$ZrO(OH)_2$	Н	IfO(OH) <sub>2</sub>
Bond	X-ray	X-ray	PDF
M-O(1)	1.859(20)	1.912(25)	2.231(2)
M-O(1)	2.334(20)	2.302(17)	2.264(7)
M-O(2)	2.045(18)	2.062(19)	2.077(1)
M-O(2)	2.000(15)	2.119(15)	2.126(3)
M-O(3)	2.284(12)	2.362(17)	2.294(6)
M-O(4),O(3)	2.2020(15)	2.294(17)	2.112(4)
	2.121	2.175	2.185
	0.19	0.18	0.09

*Note.* Average values are given in boldface, the relative degree of distortion of octahedral in italic.

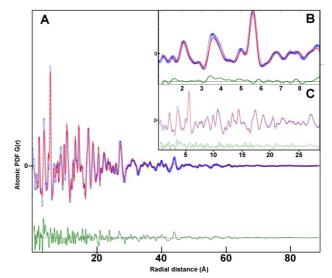


Fig.9 Experimental (circles) and model (lines) atomic PDFs G(r) for HfO(OH)<sub>2</sub>: (a) the whole range, (b)refined in the range r = 1-8 Å, (c) enlargement from (a) in the range r = 1-30 Å The residual difference between the experimental data and the model data is given in the lower part of each plot. The goodness of fit is  $R_w = 26.3\%$ .

#### 40 Conclusions

Two new solid oxyhydroxides of the IVB group of the periodic table,  $MO(OH)_2$  (M = Zr, Hf), have been synthesised by an ionexchange reaction from Li<sub>2</sub>MO<sub>3</sub> (M = Zr, Hf) precursors and their crystal structure has been solved and refined for the first <sup>45</sup> time. It has been shown that use of citrate combustion method for synthesis of precursors leads to obtaining nano-/sub-micron particles with structural defects, these two factors appear to be essential for completing the process of ion exchange and formation of MO(OH)<sub>2</sub> (M = Zr, Hf). Crystal structures of <sup>50</sup> oxyhydroxides keeps the basic motif of the related salts and can be described as a framework formed by pairs of edge-sharing MO<sub>6</sub> octahedra connected to each other via vertices. XRD, PDF and Raman experiments indicate the presence of two nonequivalent OH groups in the structure and preservation of a structural disorder. However, in order to make a solid conclusion about the origin of the disorder in both salts and oxyhydroxides

<sup>5</sup> additional state-of the- art experiments are required. Judging from the value of the chemical shift in NMR spectra and positions of the lines onIR spectra we can conclude that the acidic nature of structural OH-groups in oxyhydroxides within the IVB group of the periodic table decreases in the series Ti - Zr - Hf.

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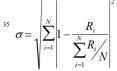
#### Notes and references

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The relative degree of the distortion is expressed by:



where N = coordination number (6 for an octahedron),  $R_i = \text{metal-oxygen}$  distance.

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